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#### Outline



2 Theory of a non-blocking I/O benchmark

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3 The benchmark and results

#### 4 Future work

#### - Motivation

### Performance improvements

In the computation environment:

- Hardware setup
- MPI distribution
- Parallel file system
- Different tuning options inside the software layers

Inside the application:

- Workload distribution
- Organization of individual program steps
- Non-blocking MPI operations

- Motivation

## Performance analysis

In order to improve performance, one needs to

- understand a complex system,
- deal with a lot of unknowns, and
- evaluate a possible margin of profit.

 $\Rightarrow$  Benchmarks are needed.

└─ Theory of a non-blocking I/O benchmark

### 1 Motivation

### 2 Theory of a non-blocking I/O benchmark

3 The benchmark and results

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## Possible scenarios

Consider a program which ...

- produces data iteratively,
- does not perform write operations on the data for a while and
- has access to non-blocking I/O functions.



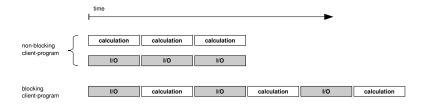
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 $\Rightarrow$  Hide I/O or calculation behind the other part respectively. Sequential operations become concurrent operations.

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### Scenarios

The most promising scenario is when I/O and calculation can be overlapped perfectly:



Any other iterative scenario can only save less time.

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### Evaluation value

#### Non-blocking efficiency ratio:

$$0.5 \leq rac{ ext{duration of non-blocking I/O version}}{ ext{duration of blocking I/O version}} (\leq 1.0)$$
 (1)

The actual value will quantify the overhead necessary to execute I/O and calculation concurrently.

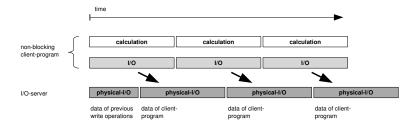
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### Desired scenario

#### We want a scenario which

- in theory promises best results, and
- requires the file system to do physical I/O as much as possible.

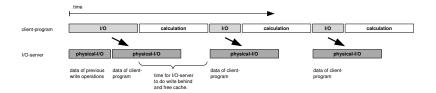


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## Expected blocking I/O version

- Time on the I/O-server side to free I/O cache
- Shorter execution time of calculation and I/O parts individually



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### Benchmark goal

Overall, the interest is in

- providing best insight into the actual possible advantages of non-blocking I/O and
- showing how close the used software can get to the optimal efficiency ratio for an optimal scenario.

### 1 Motivation

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### Benchmark details

Benchmark sequence:

Compute necessary workload so that in the non-blocking version I/O and calculation take the same amount of time

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- 2 Run non-blocking test
- 3 Run blocking test

Before each phase fill file system buffer.

## Computing environment

#### Hardware:

9 nodes with

- Two Intel Xeon 2GHz CPUs
- IGB DDR-RAM
- 1-GBit/s-Ethernet-Interfaces
- 5 I/O nodes used for hosting the pvfs2-servers, each with:

• two 160 GB S-ATA HDDs set up as a RAID-0.

## Computing environment

#### Software:

- MPICH2 in version: mpich2-1.0.5p4 non-blocking functions emulated using threads
- PVFS2 in version 2.6.2

For visualization of the benchmark behavior we used PIOviz, which includes a modified MPE trace and extended Jumpshot.

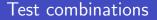
# Computing environment

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The benchmark and results



Executed tests include the combinations of:

Number CPUs per benchmark process: 1, 2

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- Number benchmark processes: 1,2,4
- Number I/O-servers: 1,2,4

The benchmark and results

### Test combinations...

2 CPUs per benchmark process in order to ignore possible overhead.

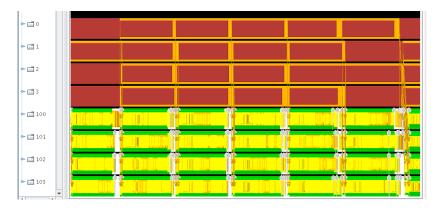
These test showed that theoretical optimum can nearly be achieved:

non-blocking efficiency ratio = 
$$0.53$$
 (2)

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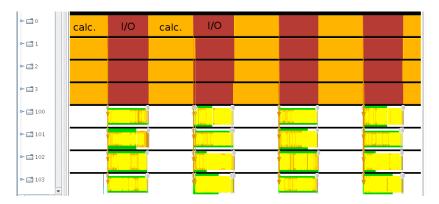
# Non-blocking I/O test

4 CPUs, 4 benchmark processes, 4 I/O-servers



# Blocking I/O test

### 4 CPUs, 4 benchmark processes, 4 I/O-servers



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### Scenario results

In average over a series of test runs we have:

```
non-blocking efficiency ratio = 0.67 (3)
```

In the non-blocking I/O test,

- the calculation time increases by a factor of 1.25 and
- the I/O time increases by a factor of 1.29

compared to the times needed for each in the blocking I/O test.

### Overall results...

For all interesting cases with 1CPU per benchmark process we obtained:

```
non-blocking efficiency ratio < 0.75 (4)
```

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Allowing for the individual parts to take longer in the non-blocking version.

Future work

# Conclusion

While we only looked at:

- write operations and
- scenarios well suited for the use of non-blocking I/O,

non-blocking I/O operations show potential to reduce execution times of HPC applications.

- Performance improvements with non-blocking I/O is possible with the used computing environment.
- Measurements suggest that short I/O phases can be hidden entirely behind longer calculation phases.

Future work



Interesting will also be an analysis of

- read operations,
- large scale tests,
- scenarios where either calculation or I/O take up the bulk of the execution time.

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